

Pascal's Triangle is a triangular array of the binomial coefficients. It is named after the French mathematician Blaise Pascal. Pascal's triangle determines the coefficients which arise in binomial expansions.

Example 1: Expand $(x+2)^4$

$$\begin{aligned} & \underline{1} (x)^4 (\cancel{2}) + \underline{4} (x)^3 (2)^1 + \underline{6} (x)^2 (2)^2 \\ & + \underline{4} (x)^1 (2)^3 + \underline{1} (\cancel{x}) (2)^4 \end{aligned}$$

$$x^4 + 8x^3 + 24x^2 + 32x + 16$$

Example 2: Expand $(x-3)^4$

$$\begin{aligned} & \underline{1} (x)^4 (\cancel{-3}) + \underline{4} (x)^3 (\cancel{-3})^1 + \underline{6} (x)^2 (\cancel{-3})^2 \\ & + \underline{4} (x)^1 (\cancel{-3})^3 + \underline{1} (\cancel{-3})^4 \end{aligned}$$

$$x^4 - 12x^3 + 54x^2 - 108x + 81$$

Example 3: Expand $(x+4)^5$

$$\begin{aligned} & \underline{1} (x)^{\cancel{5}} (\cancel{4})^{\cancel{0}} + \underline{5} (x)^{\cancel{4}} (\cancel{4})^{\cancel{1}} + \underline{10} (x)^{\cancel{3}} (\cancel{4})^{\cancel{2}} \\ & + \underline{10} (x)^{\cancel{2}} (\cancel{4})^{\cancel{3}} + \underline{5} (x)^{\cancel{1}} (\cancel{4})^{\cancel{4}} + \underline{1} (\cancel{x})^{\cancel{0}} (\cancel{4})^{\cancel{5}} \end{aligned}$$

$$\underline{1} x^5 + \underline{20} x^4 + \underline{160} x^3 + \underline{640} x^2 + \underline{1280} x + \underline{1024}$$

Example 4: What is the x^4 term in the expansion of $(3x-2)^8$?

$$\underline{70} (3x)^4 (-2)^4$$

$$70 \cdot 3^4 \cdot (-2)^4 x^4$$

$$90720 x^4$$

Example 5: What is the x^3 term in the expansion of $(2x+3)^5$?

$$\underline{10} (2x)^3 (3)^2$$

$$\underline{10 \cdot 2^3 \cdot 3^2 x^3}$$

$$720x^3$$

Example 6: What is the x^3 term
in the expansion of $(2x+10)^5$?

Left to reader